Constraint Specialisation in Horn Clause Verification

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Abstract
We present a method for specialising the constraints in constrained Horn clauses with respect to a goal. We use abstract interpretation to compute a model of a query-answer transformation of a given set of clauses and a goal. The effect is to propagate the constraints from the goal top-down and propagate answer constraints bottom-up. Our approach does not unfold the clauses at all; we use the constraints from the model to compute a specialised version of each clause in the program. The approach is independent of the abstract domain and the constraints theory underlying the clauses. Experimental results on verification problems show that this is an effective transformation, both in our own verification tools (convex polyhedra analyser) and as a pre-processor to other Horn clause verification tools.

Categories and Subject Descriptors CR-number [subcategory]: third-level

Keywords constraint specialisation; query-answer transformation; Horn clauses; abstract interpretation; convex polyhedral analysis

1. Introduction
In this paper, we present a method for specialising the constraints in constrained Horn clauses with respect to a goal. To this end, we first compute a query-answer transformation of a given set of clauses (also called a constraint logic program) with respect to a goal; the aim of the transformation is to simulate the top-down evaluation of the clauses in a bottom-up framework. Then we use abstract interpretation to compute a model of the query-answer transformed program. The idea is to propagate the constraints from the goal top-down and propagate answer constraints bottom-up. Finally we compute a specialised version of each clause in the original program using the constraints from the model without unfolding the clauses at all.

As a result, each clause is further strengthened or removed altogether, preserving the derivability of the goal. Static analysis of the specialised program becomes easier since the implicit constraints in the original clauses are made explicit in the specialised version. In addition to this, since the specialised clauses are more constrained or more specific than the original ones, more specific information will be available for proving the given goal or a failure to prove the goal may be detected at an early stage.

The approach is independent of the abstract domain and the constraints theory. Query-answer transformations, closely related to so-called “magic set” transformations, have been used for data- and query processing and logic program analysis since the 1980s [3, 16], but have not, to our knowledge, been applied to verification problems. Experimental results on verification problems show that this is an effective transformation, propagating information both backwards from the statement to be proved, and forwards from the Horn clause theory. We show its effectiveness both in our own verification tools and as a pre-processor to other Horn Clause Verification tools. In particular, we run our specialisation procedure as a pre-processor both to our convex polyhedra analyser and to QARM [24, 43], a state of the art verification tool. We make the following contributions in this paper:

- we present a method for specialising the constraints in the clauses using query-answer transformation and abstract interpretation (see Section 4); and
- we demonstrate the effectiveness of transformation by applying it to Horn clause verification problems (see Section 6).

2. Preliminaries
A constrained Horn clause (CHC) is a first order predicate logic formula of the form $\forall \phi \land p_1(X_1) \land \ldots \land p_k(X_k) \rightarrow p(X)$ ($k \geq 0$), where $\phi$ is a conjunction of constraints with respect to some background theory. $X_1, X$ are (possibly empty) vectors of distinct variables, $p_1, \ldots, p_k, p$ are predicate symbols. $p(X)$ is the head of the clause and $\phi \land p_1(X_1) \land \ldots \land p_k(X_k)$ is the body.

Pure constraint logic programs (CLP) are syntactically and semantically the same as CHC. Unlike CLP, CHCs are not always regarded as executable programs, but rather as specifications or semantic representations of other formalisms. However these are only pragmatic distinctions and the semantic equivalence of CHC and CLP means that techniques developed in one framework are applicable to the other. We follow the syntactic conventions of CLP and write a Horn clause as $p(X) \leftarrow \phi, p_1(X_1), \ldots, p_k(X_k)$. In this paper we take the constraint theory to be linear arithmetic with the relation symbols $\leq, \geq, <, >$ and $=$, but the contributions of the paper are independent of the constraint theory.

2.1 Interpretations and models
An interpretation of a set of CHCs is a truth assignment to each atomic formula $p(a_1, \ldots, a_n)$ where $p$ is a predicate and $a_1, \ldots, a_n$ are constants from the constraint theory. An interpretation is represented as a set of constrained facts of the form $A \leftarrow \phi$ where $A$ is an atomic formula $p(Z_1, \ldots, Z_n)$ where $Z_1, \ldots, Z_n$ are distinct variables and $\phi$ is a constraint over $Z_1, \ldots, Z_n$. If $\phi$ is true we write $A \leftarrow$ or just $A$. The constrained fact $A \leftarrow \phi$ is

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shorthand for the set of variable-free facts $A \theta$ such that $\phi \theta$ holds in the constraint theory, and an interpretation $M$ denotes the set of all facts denoted by its elements; $M$ assigns true to exactly those facts. $M_1 \subseteq M_2$ if the set of denoted facts of $M_1$ is contained in the set of denoted facts of $M_2$.

**Minimal models.** A model of a set of CHCs is an interpretation that satisfies each clause. There exists a minimal model with respect to the subset ordering, denoted $M[P]$ where $P$ is the set of CHCs. $M[P]$ can be computed as the least fixed point (ifp) of an immediate consequences operator (called $S^D_0$ in [28, Section 4]), which is an extension of the standard $T$ operator from logic programming, extended to handle the constraint domain $D$. Furthermore ifp($S^D_0$) can be computed as the limit of the ascending sequence of interpretations $\emptyset, S^D_0(\emptyset), S^D_0(S^D_0(\emptyset)), \ldots$. This sequence provides a basis for abstract interpretation of CHC clauses.

3. **Abstract Interpretation**

Abstract interpretation [11] is a static program analysis technique which derives sound overapproximations of programs by computing abstract fixed points. Convex polyhedra analysis (CPA) [13] is a program analysis technique based on abstract interpretation [11]. When applied to a set of CHCs $P$ it constructs an over-approximation $M'$ of the minimal model of $P$, where $M'$ contains at most one constrained fact $p(X) \not\iff \phi$ for each predicate $p$. The constraint $\phi$ is a conjunction of linear inequalities, representing a convex polyhedron.

The first application of convex polyhedra analysis to CHCs was by Benoy and King [4]. We summarise briefly the elements of convex polyhedra analysis for CHC; further details (with application to CHC) can be found in [4, 13]. Let $A$ be the set of convex polyhedra (for some fixed dimension). Let $P$ be a set of CHCs. Suppose there are $n$ predicates in $P$, say $p_1, \ldots, p_n$, and assume to simplify the discussion that all predicates have the same arity (the dimension of $A$). The abstract domain for $P$ is the set of $n$-tuples of convex polyhedra $A^n$. Let the empty polyhedron be denoted $\bot$. Inclusion of polyhedra is a partial order on $A$ and the partial order $\subseteq$ on $A^n$ is its pointwise extension. Given an element $(a_1, \ldots, a_n) \in A^n$, define the concretisation function $\gamma$ such that $\gamma((a_1, \ldots, a_n)) = \{p(a_1), \ldots, p(a_n)\}$. $\gamma$ is a point in $a_i$ in $d_{i\leq n}$. Construct an abstract semantic function $F : A^n \rightarrow A^n$ satisfying the safety condition $S^D_0(\gamma) \subseteq \gamma(F)$ which is monotonic with respect to $\subseteq$, where $S^D_0$ is the immediate consequences operator mentioned above. Let the increasing sequence $Y_0, Y_1, \ldots$ be defined as follows, $Y_0 = \bot^n, Y_{i+1} = F(Y_i)$. These conditions are sufficient to establish that if the limit of the sequence exists, say $Y$, then $M[P] = \text{ifp}(S^D_0) \subseteq \gamma(Y)$ [12].

Since $A^n$ contains infinite increasing chains, the sequence can be infinite. The use of a widening operator for convex polyhedra [11, 13] is needed to ensure convergence of the abstract interpretation. Define the sequence $Z_0 = Y_0, Z_{n+1} = Z_n \mathcal{N}F(Z_n)$ where $\mathcal{N}$ is a widening operator for convex polyhedra [13]. The conditions on $\mathcal{N}$ ensure that the sequence stabilises; thus for some finite $j$, $Z_i = Z_j$ for all $i > j$ and furthermore $Z_j$ is an upper bound for the sequence $\{Y_i\}$. The value $Z_j$ thus represents, via the concretisation function $\gamma$, an over-approximation of the least model of $P$. Furthermore much research has been done on improving the precision of widening operators. One technique is known as widening-upto, or widening with thresholds [27]. A threshold is an assertion that is combined with a widening operator to improve its precision. Recently, a technique for deriving more effective thresholds was developed [34], which we have adapted and found to be very effective in experimental studies. In brief, the method collects constraints by iterating the concrete immediate consequence func-

4. **Specialisation by constraint propagation**

We next present a procedure for specialising CHCs. In contrast to classical specialisation techniques based on partial evaluation with respect to a goal, the specialisation does not unfold the clauses at all; rather, it computes a specialised version of each clause, in which the constraints from the goal are propagated top-down and answers are propagated bottom-up.

We first make precise what is meant by “specialisation” for CHCs. Let $P$ be a set of CHCs and let $A$ be an atomic formula. The specialisation of $P$ with respect to $A$ is a set of clauses $P_A$ such that for every constraint $\phi$ over the variables of $A$, $P \models \forall(\phi \rightarrow A)$ if and only if $P_A \models \forall(\phi \rightarrow A)$. This is a very general definition which allows for many transformations. In practice we are interested in specialisations that eliminate consequences of $P$ that have no relevance to $A$.

For each clause $H \leftarrow B$ in $P$, $P_A$ contains a new clause $H \leftarrow \phi, B$ where $\phi$ is a constraint. If the addition of $\phi$ makes the clause body unsatisfiable, it is the same as removing the clause. Clearly $P_A$ may have fewer consequences than $P$ but our procedure guarantees that it preserves the inferability of (constrained instances of) $A$. The procedure is summarised as follows: the inputs are a set of CHCs $P$ and an atomic formula $A$.

1. Compute a query-answer transformation of $P$ with respect to $A$, denoted $P^{qa}$, containing predicates $p^1$ and $p^2$ for each predicate $p$ in $P$.

2. Compute an over-approximation $M$ of the model of $P^{qa}$.

3. Strengthen the constraints in the clauses in $P$, by adding constraints from the answer predicates in $M$.

Next we will explain each step in detail.

4.1 The query-answer transformation

The query-answer transformation in CLP was inspired by the magic-set transformation from deductive databases and the language Datalog [3]. Its purpose, both in deductive databases and in subsequent applications in logic program analysis [16] was to simulate goal-directed (top-down) computation or deduction in a goal-independent (bottom-up) framework.

In the following, for each atom $A = p(t)$, $A^a$ and $A^s$ represent the atoms $p^s(t)$ and $p^a(t)$ respectively. Given a set of CHCs $P$ and an atom $A$, the (left-) query-answer clauses for $P$ with respect to $A$, denoted $P^{qa}_A$ or just $P^{qa}$, are as follows.

- (Answer clauses). For each clause $H \leftarrow \phi, B_1, \ldots, B_n$ ($n \geq 0$) in $P$, $P^{qa}$ contains the clause $H^a \leftarrow \phi, H^a, B_1^a, \ldots, B_n^a$.

- (Query clauses). For each clause $H \leftarrow \phi, B_1, \ldots, B_n$ ($n \geq 0$) in $P$, $P^{qa}$ contains the following clauses:

  - $B_1^a \leftarrow \phi, H^a$.
  - $B_2^a \leftarrow \phi, H^a, B_1^a, \ldots, B_{i-1}^a$.
  - $\ldots$ $B_n^a \leftarrow \phi, H^a, B_1^a, \ldots, B_{n-1}^a$.

- (Goal clause). $A^s \leftarrow true$.

The clauses $P^{qa}$ encodes a left-to-right, depth-first computation of the query $\leftarrow A$ for CHC clauses $P$ (that is, the standard CLP computation rule, SLD extended with constraints). This is a complete proof procedure, assuming that all clauses matching a given call are explored in parallel. (Note: the incompleteness of standard Prolog
CLP proof procedures arises due to the fact that clauses are tried in a fixed order). It is important to generate the queries and answers in a single set of clauses, since in general the predicates \( p^2 \) and \( p^2 \) are mutually recursive. Independent analyses propagating constraints from head to body of the clauses and propagating constraints from body to head would not in general achieve the same specialisation.

The relationship of the model of the clauses \( P^{\text{oa}} \) to the computation of the goal \( A \) in \( P \) is expressed by the following property 1. An SLD-derivation in \( C \) is a sequence \( G_0, G_1, \ldots, G_k \) where each \( G_i \) is a goal \( \leftarrow \phi, B_1, \ldots, B_m, \) where \( \phi \) is a constraint and \( B_1, \ldots, B_m \) are atoms. In a left-to-right computation, \( G_{i+1} \) is obtained by resolving \( B_1 \) with a program clause. The model of \( P^{\text{oa}} \) captures the set of atoms that are called or queried during the derivation, together with the answers (if any) for those calls. This is expressed precisely by Property 1.

**Property 1** (Correctness of query-answer transformation). Let \( P \) be a set of CHCs and \( A \) be an atom. Let \( P^{\text{oa}} \) be the query-answer program for \( P \) w.r.t. \( A \). Then

1. **(i)** if there is an SLD-derivation \( D_0, \ldots, D_m \) where \( D_0 = A \) and \( D_i \leftarrow \phi, B_1, \ldots, B_m \), then \( P^{\text{oa}} \models \phi \leftarrow B_1 \).
2. **(ii)** if there is an SLD-derivation \( D_0, \ldots, D_m, D_{m+1} \) where \( D_0 = A \), containing a sub-derivation \( D_j_1, \ldots, D_j_k \), where \( D_{j_i} \leftarrow \phi_i, B_i, B_i' \), then \( P^{\text{oa}} \models \phi_i \leftarrow B_i \). (This means that the atom \( B_i \) in \( D_{j_i} \) was successfully answered, with answer constraint \( \phi_i \leftarrow B_i \).
3. **(iii)** As a special case of (ii), if there is a successful derivation of the goal \( \leftarrow A \) with answer constraint \( \phi \) then \( P^{\text{oa}} \models \phi \leftarrow A \).

Variations such as the following have been used.

- (Refined call predicates). Call predicates of the form \( p^k_{i,j} \) could be generated representing calls to the \( j \)-th atom in the body of clause \( j \) [20], giving more fine-grained information on calls.
- (Relaxed answer predicates). In this version the answer clauses are the same as the original clauses of \( p \), and every answer predicate \( p^2 \) is just replaced by \( p \). This can be used where the only interest is in the model of the query predicates, and the motivation is to increase efficiency of analysis of \( P^{\text{oa}} \), while possibly losing precision [9].

**5. Application to the CHC verification problem**

In this section, we discuss the application of our constraint specialisation in Horn clause verification. We assume that there is a distinguished predicate symbol false in \( P \) which is always interpreted as false. In practice the predicate false only occurs in the head of clauses; we call clauses whose head is true integrity constraints, following the terminology of deductive databases. This is equivalent to the formula \( \neg \phi \). The latter might not be a CHC (e.g. if \( \phi \) contains \( = \) but can be converted to an equivalent set of CHCs by transforming the formula \( \neg \phi \) and distributing any disjunctions that arise over the rest of the body. For example, the formula \( X = Y \leftarrow p(X, Y) \) is equivalent to the set of CHCs \( \{ \neg X \leftarrow Y, p(X, Y), \neg X \leftarrow Y, p(X, Y) \} \).

Integrity constraints can be seen as safety properties. For example if a set of CHCs encodes the behaviour of a transition system, the bodies of integrity constraints represent unsafe states. Thus
proving safety consists of showing that the bodies of integrity constraints are false in all models of the CHC clauses. Figure 1 shows an example set of CHCs taken from [23].

c6. l_body(A,B,C,D) :- A-C= -2,B-D= -1.
c5. l_body(A,B,C,D) :- A-C= -1,B-D= -2.
c3. l(A,B,C,D) :- A-D>=0,B+C-3*D>0.
c1. false :- A>0,B=0,C=0,D=0,l(B,C,D,A).

An example set of CHCs taken from [23].

It is sufficient to find a set of constrained facts entailed false. The constraint strengthening procedure described in Section 4 is our method of specialisation.

Consider the application of the procedure in Section 4 to the clauses in Figure 1, where the query-answer transformation is performed with respect to the atom false. The result is shown in Figure 2. Note that the constraint in clause c4 is strengthened to false, showing that c4 is definitely not used in any derivation of false (and hence can be removed).

c1. false :- A>0,B=0,C=0,D=0,l(B,C,D,A).
c2. l(A,B,C,D) :- 2*A-B>=0,-A+D>=0,-A+B>=0,3*A-A-B>=0, A-G= -1,l_body(B,C,E,F),l(G,E,F,D).
c3. l(A,B,C,D) :- A-D>=0,-A+B>=0,2*A-B>=0,-A+D= -1, A+B>=0,3*A-B=C=0.
c4. l(A,B,C,D) :- false.
c5. l_body(A,B,C,D) :- -A+2*B>=0,2*A-B>=0, A-C= -1,B-D= -2.

Figure 1. Example program t4.pl [23]

Figure 2. Example program t4.pl [23] with strengthened constraints

5.1 The CHC verification problem.

To state this more formally, given a set of CHCs P, the CHC verification problem is to check whether there exists a model of P. If so we say that P is safe. Obviously any model of P assigns false to the bodies of integrity constraints. We restate this property in terms of the logic consequence relation. Let P |= P′ mean that P is a logical consequence of P′, that is, that every interpretation satisfying P also satisfies P′.

LEMMA 1. P has a model if and only if P |= false.

This lemma holds for arbitrary interpretations (only assuming that the predicate false is interpreted as false), uses only the textbook definitions of “interpretation” and “model” and does not depend on the constraint theory.

The verification problem can be formulated deductively rather than model-theoretically. We can exploit proof procedures for constraint logic programming [28] to reason about the satisfiability of a set of CHCs. Let the relation P |= A denote that A is derivable from P using some proof procedure. If the proof procedure is sound then P |= A implies P |= A, which means that P = false is a sufficient condition for P to have no model, by Lemma 1. This corresponds to using a sound proof procedure to find or check a counterexample. On the other hand to show that P does have a model, soundness is not enough since we need to establish P |= false. As we will see in Section 5.2 we approach this problem by using approximations to reason about the non-provability of false, applying the theory of abstract interpretation [10] to a complete proof procedure for atomic formulas (the “fixed-point semantics” for constraint logic programs [28, Section 4]). In effect, we construct by abstract interpretation a proof procedure that is complete (but possibly not sound) for proofs of atomic formulas. With such a procedure, P |= false implies P |= false and thus establishes that P has a model.

5.2 Proof Techniques

Proof by over-approximation of the minimal model. It is a standard theorem of CLP that the minimal model M[P] is equivalent to the set of atomic consequences of P. That is, P |= p(v1, . . . , vn) if and only if p(v1, . . . , vn) ∈ M[P]. Therefore, the CHC verification problem for P is equivalent to checking that false /∈ M[P]. It is sufficient to find a set of constrained facts M′ such that M[P] ⊆ M′, where false /∈ M′. This technique is called proof by over-approximation of the minimal model.

Proof by specialisation. A specialisation of a set of CHCs P with respect to an atom A is the transformation of P to another set of CHCs P′ such that P |= A if and only if P′ |= A. In our context we use specialisation to focus the verification problem on the formula to be proved. More specifically, we specialise a set of CHCs with respect to a “query” to the atom false; thus the specialised CHCs entail false if and only if the original clauses entailed false.
The results show that constraint specialisation is effective in practice. We report that 109 out of 218, that is 50%, of the problems are solved by constraint specialisation alone. When used as a pre-processor for other verification tools, the results show improvements on both the number of instances solved and the solution time. Using our tool, we report approximately 47% increase in the number of instances solved and twice as much faster in average. Similarly using QARMC, we report 13% increase in the number of instances solved and 5 times faster in average.

<table>
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<td>125/141/157</td>
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Table 1. Experiments on a set of 218 (181 safe and 37 unsafe) 
CHC verification problems

The (perhaps surprising) effectiveness of this relatively simple combination of specialisation and convex polyhedral analysis is underlined by noting that it can solve problems for which more complex methods have been proposed. For example, apart from the many examples from the Horn clause verification benchmarks that require refinement using CEGAR-based approaches, the technique solves the “rate-limiter” and “Boustrophedon” examples presented by Monniaux and Gonnord [40] (Section 5) (directly encoded as Horn clauses); their approach, also based on convex polyhedra, uses bounded model checking to achieve a partitioning of the approximation, while other approaches to such problems use trace-partitioning and look-ahead widening.

7. Related Work

Techniques for strengthening the constraints of logic programs go back at least to the work of Marriott et al. on most specific logic programs [39]. In that work the constraints were just equalities between terms and the strengthening was goal-independent. In [19] the idea was similar but it was extended to strengthen constraints while preserving the answers with respect to a goal.

The partial evaluation of (constraint) logic programs also has a long history [17, 18, 30, 32]. The aim is to specialise a program with respect to a goal, but usually unfolding is the key technique for propagating constraints. Global analysis using abstract interpretation was combined with partial evaluation algorithms to propagate constraints bottom-up as well as top-down [22, 31, 33, 35, 36].

Abstract interpretation over the domain of convex polyhedra was introduced by Cousot and Halbwachs [13] and applied to constraint logic programs by Benoy and King [4]. Abstract interpretation over convex polyhedra was incorporated in a program specialisation algorithm by Peralta and Gallagher [41].

The method of widening with thresholds for increasing the precision of widening convex polyhedra was first presented by Halbwachs et al. [27]. We applied a technique for generating threshold constraints presented by Lakhdar-Chaouch et al. [34].

In summary, the basic specialisation techniques that we apply are well known, though we are not aware of previous work combining them in the same way. Our method is a specialisation with respect to a goal but does not perform partial evaluation by unfolding. The aim of our specialisation is to make constraints explicit and propagate constraints as much as possible, thereby making other tools more effective, rather than to produce a more efficient computation of a goal.

Verification of CLP programs using abstract interpretation and specialisation has been studied for some time. Our aim in this paper is not to demonstrate a verification tool but to identify a transformation that benefits CLP verification tools generally.

The idea of improving analysis by applying it to a specialised program was first expressed by Turchin [44] and it was more recently demonstrated using supercompilation [38]. The use of program transformation to verify properties of logic programs was pioneered by Pettorossi and Proietti [42] and Leusçon [37] and continues in recent work by De Angelis et al. [14, 15]. Transformations that preserve the minimal model (or other suitable models) of logic programs are applied systematically to make properties explicit.

Much other work on CLP verification exists, much of it based on property abstraction and refinement using interpolation, for example [2, 6, 8, 24, 26, 43]. Our specialisation technique is not directly comparable to these methods, but as we have shown in experiments with QARMC, constraint specialisation can be used as a pre-processor to such tools, increasing their effectiveness.

8. Conclusion and future Work

We introduced a method for specialising the constraints in constrained Horn clauses with respect to a goal using abstract interpretation and query-answer transformation. The approach propagates constraints globally, both forwards and backwards, and makes explicit constraints from the original program. This allows better analysis of the transformed program. Furthermore, our approach is independent of the abstract domain and the constraints theory underlying the clauses. Finally, we showed effectiveness of this transformation in Horn clause verification problems.

In the future, we will continue to evaluate its effectiveness in a larger set of benchmarks and as a pre-processor for other existing tools. We also would like to use the specialised version for other purposes, for instance in program debugging since more specific information may make errors in the original program apparent.

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References
